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APPLICATION NO.	FILING DATE	FIRST NAMED INVENTOR	ATTORNEY DOCKET NO.	CONFIRMATION NO.
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09/328,726

10/26/1998

THOMAS COLLINS

2026-25(PT-TA  
410(Cont1)

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25696

7590

05/06/2003

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EXAMINER

SEAL, JAMES

ART UNIT

PAPER NUMBER

2131

DATE MAILED: 05/06/2003

Please find below and/or attached an Office communication concerning this application or proceeding.

**Office Action Summary**

Application No.

09/328,726

Applicant(s)

COLLINS ET AL.

Examiner

James Seal

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-- The MAILING DATE of this communication appears on the cover sheet with the correspondence address --

**Period for Reply**

A SHORTENED STATUTORY PERIOD FOR REPLY IS SET TO EXPIRE 3 MONTH(S) FROM THE MAILING DATE OF THIS COMMUNICATION.

- Extensions of time may be available under the provisions of 37 CFR 1.136(a). In no event, however, may a reply be timely filed after SIX (6) MONTHS from the mailing date of this communication.
- If the period for reply specified above is less than thirty (30) days, a reply within the statutory minimum of thirty (30) days will be considered timely.
- If NO period for reply is specified above, the maximum statutory period will apply and will expire SIX (6) MONTHS from the mailing date of this communication.
- Failure to reply within the set or extended period for reply will, by statute, cause the application to become ABANDONED (35 U.S.C. § 133).
- Any reply received by the Office later than three months after the mailing date of this communication, even if timely filed, may reduce any earned patent term adjustment. See 37 CFR 1.704(b).

**Status**

- 1) ☒ Responsive to communication(s) filed on 05 February 2003.
- 2a) ☐ This action is **FINAL**. 2b) ☒ This action is non-final.
- 3) ☐ Since this application is in condition for allowance except for formal matters, prosecution as to the merits is closed in accordance with the practice under *Ex parte Quayle*, 1935 C.D. 11, 453 O.G. 213.

**Disposition of Claims**

- 4) ☒ Claim(s) 17-66 and 73-92 is/are pending in the application.
- 4a) Of the above claim(s) \_\_\_\_\_ is/are withdrawn from consideration.
- 5) ☐ Claim(s) \_\_\_\_\_ is/are allowed.
- 6) ☒ Claim(s) 17-66 and 73-92 is/are rejected.
- 7) ☐ Claim(s) \_\_\_\_\_ is/are objected to.
- 8) ☐ Claim(s) \_\_\_\_\_ are subject to restriction and/or election requirement.

**Application Papers**

- 9) ☐ The specification is objected to by the Examiner.
- 10) ☐ The drawing(s) filed on \_\_\_\_\_ is/are: a) ☐ accepted or b) ☐ objected to by the Examiner.
- Applicant may not request that any objection to the drawing(s) be held in abeyance. See 37 CFR 1.85(a).
- 11) ☐ The proposed drawing correction filed on \_\_\_\_\_ is: a) ☐ approved b) ☐ disapproved by the Examiner.
- If approved, corrected drawings are required in reply to this Office action.
- 12) ☐ The oath or declaration is objected to by the Examiner.

**Priority under 35 U.S.C. §§ 119 and 120**

- 13) ☒ Acknowledgment is made of a claim for foreign priority under 35 U.S.C. § 119(a)-(d) or (f).
- a) ☐ All b) ☐ Some \* c) ☐ None of:
1. ☐ Certified copies of the priority documents have been received.
2. ☐ Certified copies of the priority documents have been received in Application No. \_\_\_\_\_.
3. ☐ Copies of the certified copies of the priority documents have been received in this National Stage application from the International Bureau (PCT Rule 17.2(a)).
- \* See the attached detailed Office action for a list of the certified copies not received.
- 14) ☒ Acknowledgment is made of a claim for domestic priority under 35 U.S.C. § 119(e) (to a provisional application).
- a) ☐ The translation of the foreign language provisional application has been received.
- 15) ☐ Acknowledgment is made of a claim for domestic priority under 35 U.S.C. §§ 120 and/or 121.

**Attachment(s)**

- 1) ☒ Notice of References Cited (PTO-892)
- 2) ☐ Notice of Draftsperson's Patent Drawing Review (PTO-948)
- 3) ☐ Information Disclosure Statement(s) (PTO-1449) Paper No(s) \_\_\_\_\_.
- 4) ☐ Interview Summary (PTO-413) Paper No(s). \_\_\_\_\_.
- 5) ☐ Notice of Informal Patent Application (PTO-152)
- 6) ☐ Other: \_\_\_\_\_.

### **DETAILED ACTION**

1. The request filed on 05 February 2003 for a request for Continued Examination (RCE) under 35 CFR 132 based on Parent Application No. 09/328726 is acceptable and an RCE has been established. An Action on the RCE follows.
2. Claims 14-16 have been cancelled without prejudice.
3. Claims 17, 22, 27, 32, 37, 42, 47, 52, 57, and 62 have been amended.
4. Claims 17-66 and 73-92 are pending.

#### ***Docketing***

5. Please note that the application has been redocketed to a different examiner. Please refer all future communications regarding this application to the examiner of record, using the information supplied in the final section of the office action.

#### ***Claim Rejections - 35 USC § 112***

6. With the amendments and claim cancellation all 112 are withdrawn in the previous Action.

#### ***Specification***

7. The title of the invention is not descriptive. A new title is required that is clearly indicative of the invention to which the claims are directed. Examiner suggest "A Multiprime RSA Public Key Cryptosystem".

#### ***Drawings***

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8. This application has been filed with informal drawings which are acceptable for examination purposes only. Formal drawings will be required when the application is allowed.

***Claim Rejections - 35 USC § 103***

The following is a quotation of 35 U.S.C. 103(a) which forms the basis for all obviousness rejections set forth in this Office action:

(a) A patent may not be obtained though the invention is not identically disclosed or described as set forth in section 102 of this title, if the differences between the subject matter sought to be patented and the prior art are such that the subject matter as a whole would have been obvious at the time the invention was made to a person having ordinary skill in the art to which said subject matter pertains. Patentability shall not be negated by the manner in which the invention was made.

9. Claim 17 is rejected under 35 U.S.C. 103(a) as being unpatentable over Lidl and Pilz (Applied Abstract Algebra, 1984), and further in view of Quisquater and Couvreur, Fast Decipherment Algorithm for RSA Public –Key Cryptosystem, 1982) and Rivest et. al. A Method for Obtaining Digital Signatures and Public-key Cryptosystem, Communications of the ACM, 21(2) February 1978, henceforth Rivest.

10. As per claim 1, the limitation of a cryptographic system which breaks messages into blocks  $M$  of size  $0 \leq M \leq n$  where  $n$  is a modulus of an RSA encryption algorithm

$$C \equiv M^e \pmod{n}$$

$$M \equiv C^d \pmod{n}$$

$$ed \equiv 1 \pmod{\lambda(n)}$$

the latter would imply

$$d \equiv e^{-1} \pmod{\lambda(n)}$$

such that  $n \in \mathbb{Z}$  with prime factorization

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$$n = p_1^{e_1} p_2^{e_2} p_3^{e_3} \dots p_k^{e_k}$$

$$\lambda(n) = \text{lcm} \{ \lambda(p_1^{e_1}) \lambda(p_2^{e_2}) \lambda(p_3^{e_3}) \dots \lambda(p_k^{e_k}) \}$$

for which if  $e_i > 2$ 

$$\lambda(p_i^{e_i}) = \phi(p_i^{e_i})$$

is the Euler totient and if  $e_i = 1$ 

$$\phi(p_i) = p_i - 1$$

with  $e$  relatively primed to  $(p_1 - 1)(p_2 - 1)(p_3 - 1) \dots (p_k - 1)$  which would imply

$$d \equiv e^{-1} \pmod{\{(p_1 - 1)(p_2 - 1)(p_3 - 1) \dots (p_k - 1)\}}$$

Is disclosed in Lidl page 289, lines 3, 5-6, bottom page 290, page 291 lines 3-7, page 293 problem 11. Lidl does not disclose the use of the Chinese Remainder Theorem (CRT) with respect to the problem at hand; however, by way of example, Lidl does teach application of his teachings to the special case of where the prime factors are distinct  $p_1 = p$  and  $p_2 = q$ , that is,  $e_1 = e_2 = 1$ .

Quisquater teaches reduction RSA (two prime factors  $p$  and  $q$ ) calculation to a simultaneous system of modular congruences

$$C_1 \equiv C \pmod{p_1}$$

$$C_2 \equiv C \pmod{p_2}$$

$$M_1 \equiv C_1^{d_1} \pmod{p_1}$$

$$M_2 \equiv C_2^{d_2} \pmod{p_2}$$

$$d_1 \equiv d \pmod{p_1 - 1}$$

$$d_2 \equiv d \pmod{p_2 - 1}$$

Solving for the results for  $M_1$  and  $M_2$  and combining the sub-task to produce the receive message  $M$ . Reducing the calculations to simultaneous sub-task allows Quisquater to carry out the calculations much faster as  $p_1$  and  $p_2$ ,  $d_1$ ,  $d_2$ ,  $M_1$ ,  $M_2$  and  $C_1$ ,  $C_2$  are much smaller in terms of the number of bits (see page 906 lines 3-8, 31-39, 55-60). Further

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such subtasks may be applied in parallel (see figure 1, for example the exponentiation modules  $x^2 \bmod p$  and  $x^2 \bmod q$  which calculate different subtasks at the same time.

Thus one of ordinary skill in the art would recognize the speed and savings in computational resources which could be derived from using the teachings of Quisquater and would be strongly motivated to apply these teaching to Lidl algorithm. Lidl pages 515-517 also teaches the generalization of the above process for the case of  $k$  factors.

Lidl is silent on the choice of the  $e_i$  's, as he is seeking to generalize the RSA system to its fullest. The RSA paper teaches both *randomness* and *distinctness* are important in the selection of primes for the two prime factors  $p$  and  $q$  scheme that they propose (see Rivest et. al. page 6, line 34 ;page 9, lines 2-3, and line 26-27) in order to maximize security. If the size of the modulus  $n$  is restricted to 200 digits, then maximum security is attained by taking by choose  $p$  and  $q$  differing by a few digits (distinctness) and choosen at random. Thus if randomness and distinctness is not applied to multifactor scheme, one losses the randomness that is there are a lot fewer ways to choose a two hundred digit number of the form  $p^2 q$  as opposed to  $pqr$  and hence a loss of security. Thus one of ordinary skill in the art would recognize in order to maximize security one must increase the number of possible choices which implies distinctness of all factors that is  $e_1 = e_2 = e_3 = \dots = e_k$  in the teaching of Lidl. Thus one of ordinary skill of the art would have been modivated to combine the general teachings of Lidl with the additional speed enhancements of Quisquater and finally the security teachings of the original RSA paper to obtain a security system which is fast and could run on devices with

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limited computational resources such as CD ROM's, smartcards, secure net browsers, etc. Claim 1 is rejected.

Claim 18-66 and 73-92 rejected under 35 U.S.C. 103(a) as being unpatentable over Lidl and Pilz (Applied Abstract Algebra, 1984), and further in view of Quisquater and Couvreur, Fast Decipherment Algorithm for RSA Public -Key Cryptosystem, 1982) and Rivest et. al. A Method for Obtaining Digital Signatures and Public-key Cryptosystem, Communications of the ACM, 21(2) February 1978, as applied to claim 17 above, and further in view of Ding et. al. The Chinese Remainder Theorem, World Scientific.

9. As per claim 18-21, the details of a recursive (iterative) algorithm is given page 23. Note the relabelling of the dummy indices and the use of the extended Euclidian algorithm  $u_i M_i + v_i m_i = 1$  to provide the inverse  $u_i$  or  $w_i^{-1}$  modulo  $m_k$  or  $p_i$  in 2.8 of the product  $M_k$  corresponding to applicant's  $w_i$ . Claims 18-21 are rejected.

10. Claims 22-26 are a system implementation of claims 17-21 and are rejected in view of the same prior art of record.

11. In claim 17, the limitation of the decomposition into subtasks performed simultaneously, of the RSA decryption equation was applied without any corresponding application of the same technique to the encryption part of the encryption system. The limitations of claims 27 are directed to the same decomposition into subtasks to be performed simultaneously. One of ordinary skill in the art recognizing the same benefits may be had by applying the same mathematics to the encryption area would have been

motivated to apply it to the encryption part of the cryptosystem to gain the same benefits. Claim 27 is rejected.

12. As per claims 28-31, expand upon the CRT algorithm applied to this aspect of the encryption and would be rejected on the same group as claims 18-21. Claims 28-31 are rejected.

13. Claims 32-36 are a system implementation of claims 27-31 and are rejected in view of the same prior art of record. Claims 27-31 are rejected.

14. Claims 37-41 and 44 recite a method for decoding corresponding to the method of encoding claims of 17-22 and are rejected in view of the same prior art (all references disclosed both an encoding and decoding scheme). Claim 37-41 and 44 are rejected.

15. As per claims 42-43, and 45-46, the limitation of a cryptographic system for decoding implementing method of claims 37-41, and 44 is rejected in view of the same prior art of record. Claims 42-41 and 44 are rejected.

16. As per claim 47-51, the limitation for a method of generating digital signature is disclosed by Rivest (see pages 4-6) for two prime factors. Using the Lidl/Quisquater/Ding scheme, one of ordinary skill in the art would have also been motivated to apply the same techniques to digital signature to increase speed, conserve computational resources which are important credit card transactions, and digital rights management. Claims 47-51 are rejected.

17. Claims 52-56 are a system implementation for the generating method recited in claims 47-52 and is rejected in view of the same prior art of record. Claims 52-56



18. As per claims 57-61, the limitations of a process for verifying digital signatures, recited in the method claims 47-52 is disclosed by Rivest (page 5). Claims 57-61 are rejected.

19. Claims 62-66, recite a system for generating and validating digital signatures corresponding to method claims 47-51 and 57-61 and are rejected in view of the same prior art of record.

20. Claims 73, 75, 77, 79, 81, 83, 85, 87, 89, 91 recites the limitation of a plurality of exponentiator units operating substantially simultaneously and performing subtasks are disclosed by Figure 1 Quisquater. Claims 73, 75, 77, 79, 81, 83, 85, 87, 89, 91 are rejected.

21. Claims 74, 76, 78, 80, 82, 84, 86, 88, 90, 92 recite the limitation that each distinct random prime factor has the same number of bits is disclosed in Quisquater page 906 second column under figure 1.

22. Claims 17 is rejected under 35 U.S.C. 103(a) as being unpatentable over Rivest et. al. (US 4,405,829 A) henceforth RSA, and further in view of Rivest et. al. A Method for Obtaining Digital Signatures and Public-key Cryptosystem, Communications of the ACM, 21(2) February 1978, henceforth Rivest, Quisquater, Fast Decipherment Algorithm for RSA Public-key Cryptosystem and further in view of Knuth, The Art of Computer Programming vol 2 page 179.

23. As per claim 17, the limitation of a method for processing messages in a communication system with RSA public key encryption an alternative embodiment of the present invention ( see Figure 6, Abstract line 1 of Column 4, lines 15 through Column 5,

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lines 11, RSA), such that three or more primes  $p_1, p_2, p_3, \dots, p_k$  are generated, such that  $k > 2$  (Column 13, lines 30-31) then using the present invention (Column 13, line 29) provided and  $e$  relatively prime to  $\phi(n)$  (Column 13, lines 42-44),  $\phi(n) = (p_1 - 1)(p_2 - 1)(p_3 - 1) \dots (p_k - 1)$ , that is, relatively prime to  $(p_1 - 1)(p_2 - 1)(p_3 - 1) \dots (p_k - 1)$  and generating from the product of these primes and integer  $n$  which will be the resulting modulus  $n$  (Column 13, line 30-31, line 34) using the provided  $e$  and  $n$  together with a message  $M$  where  $0 \leq M \leq n-1$  (Column 4, line 26), and the RSA encryption algorithm  $C \equiv M^e \text{ mod } n$  (Column 4, line 59, RSA) to generate a cipher text  $C$ , decrypting  $C$  at the intended recipient (Column 6, 29-31) having available to it. RSA suggest the CRT but is silent on the details. Quisquater provides the details and motivations (see discussion in claim 17 above) for the implementation for two parameters.

24. The RSA paper teaches both *randomness* and *distinctness* are important in the selection of primes for the two prime factors  $p$  and  $q$  scheme that they propose (see Rivest et. al. page 6, line 34 ;page 9, lines 2-3, and line 26-27) in order to maximize security. If the size of the modulus  $n$  is restricted to 200 digits, then maximum security is attained by taking by choose  $p$  and  $q$  differing by a few digits (distinctness) and chosen at random. Thus if randomness and distinctness is not applied to multifactor scheme, one losses the randomness that is there are a lot fewer ways to choose a two hundred digit number of the form  $p^2 q$  as opposed to  $pqr$  and hence a loss of security. Thus one of ordinary skill in the art would recognize in order to maximize security one must increase the number of possible choices which implies distinctness of all factors that is  $e_1 = e_2 = e_3 = \dots = e_k$ . Thus one of ordinary skill of the art would have been motivated to combine the general teachings of Lidl with the additional speed

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enhancements of Quisquater and finally the security teachings of the original RSA paper to obtain a security system which is fast and could run on devices with limited computational resources such as CD ROM's, smartcards, secure net browsers, etc.

25. RSA patent recites a different embodiment (Column 13, lines 30-31) in which the modulus  $n$  is a product of three or more primes (not necessarily distinct primes). RSA further goes on to state that decoding may be performed modulo each of the prime factors of  $n$  (thus breaking the calculations into a series of subtasks involving the factors of  $n$  and not  $n$ ) and then combining the results using "Chinese remaindering" (that is the Chinese remainder theorem henceforth CRT). However, only in the case of distinct primes can the decoding problem be performed using the CRT. In the case of non-distinct primes one would need in addition Hensel's Lemma (or a generalization by Hensel of  $p$ -adics, see Knuth vol 2, page 179). Thus it is clear that the RSA patent is referring to the case of distinct primes. Claim 1 is rejected.

26. Claim 18-66 and 73-92 rejected under 35 U.S.C. 103(a) as being unpatentable over Rivest et. al. (US 4,405,829 A) henceforth RSA, and further in view of Quisquater and Couvreur, Fast Decipherment Algorithm for RSA Public-Key Cryptosystem, 1982) and Rivest et. al. A Method for Obtaining Digital Signatures and Public-key Cryptosystem, Communications of the ACM, 21(2) February 1978, as applied to claim 17 above, and further in view of Ding et. al. The Chinese Remainder Theorem, World Scientific.

27. As per claim 18-21, the details of a recursive (iterative) algorithm is given page 23. Note the relabelling of the dummy indices and the use of the extended Euclidian

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algorithm  $u_i M_i + v_i m_i = 1$  to provide the inverse  $u_i$  or  $w_i^{-1}$  modulo  $m_k$  or  $p_i$  in 2.8 of the product  $M_k$  corresponding to applicant's  $w_i$ . Claims 18-21 are rejected.

28. Claims 22-26 are a system implementation of claims 17-21 and are rejected in view of the same prior art of record.

29. In claim 17, the limitation of the decomposition into subtasks performed simultaneously, of the RSA decryption equation was applied without any corresponding application of the same technique to the encryption part of the encryption system. The limitations of claims 27 are directed to the same decomposition into subtasks to be performed simultaneously. One of ordinary skill in the art recognizing the same benefits may be had by applying the same mathematics to the encryption area would have been motivated to apply it to the encryption part of the cryptosystem to gain the same benefits. Claim 27 is rejected.

30. As per claims 28-31, expand upon the CRT algorithm applied to this aspect of the encryption and would be rejected on the same group as claims 18-21. Claims 28-31 are rejected.

31. Claims 32-36 are a system implementation of claims 27-31 and are rejected in view of the same prior art of record. Claims 27-31 are rejected.

32. Claims 37-41 and 44 recite a method for decoding corresponding to the method of encoding claims of 17-22 and are rejected in view of the same prior art (all references disclosed both an encoding and decoding scheme). Claim 37-41 and 44 are rejected.

33. As per claims 42-43, and 45-46, the limitation of a cryptographic system for decoding implementing method of claims 37-41, and 44 is rejected in view of the same prior art of record. Claims 42-41 and 44 are rejected.

34. As per claim 47-51, the limitation for a method of generating digital signature is disclosed by Rivest (see pages 4-6) for two prime factors. Using the Lidl/Quisquater/Ding scheme, one of ordinary skill in the art would have also been motivated to apply the same techniques to digital signature to increase speed, conserve computational resources which are important credit card transactions, and digital rights management. Claims 47-51 are rejected.

35. Claims 52-56 are a system implementation for the generating method recited in claims 47-52 and is rejected in view of the same prior art of record. Claims 52-56

36. As per claims 57-61, the limitations of a process for verifying digital signatures, recited in the method claims 47-52 is disclosed by Rivest (page 5). Claims 57-61 are rejected.

37. Claims 62-66, recite a system for generating and validating digital signatures corresponding to method claims 47-51 and 57-61 and are rejected in view of the same prior art of record.

38. Claims 73, 75, 77, 79, 81, 83, 85, 87, 89, 91 recites the limitation of a plurality of exponentiator units operating substantially simultaneously and performing subtasks are disclosed by Figure 1 Quisquater. Claims 73, 75, 77, 79, 81, 83, 85, 87, 89, 91 are rejected.

39. Claims 74, 76, 78, 80, 82, 84, 86, 88, 90, 92 recite the limitation that each distinct random prime factor has the same number of bits is disclosed in Quisquater page 906 second column under figure 1.

40. Claim 17 is rejected under 35 U.S.C. 103(a) in view of Nemo, RSA Moduli Should Have 3 Primes Factors, August 1996 and Rivest et. al. A Method for Obtaining Digital Signatures and Public-key Cryptosystem, Communications of the ACM, 21(2) February 1978, henceforth Rivest and Quisquater Fast Decipherment Algorithm for RSA Public-key Cryptosystem, 1982.

41. Nemo discloses the use of a three prime RSA (see section 3). Each prime  $p$ ,  $q$ ,  $r$  would contain the same number of bits (256 bits) and the modulus  $n$  would contain 768 bits. The system would provide digital signature, encryption, decryption, and self encryption (files, backup tapes and archives) and in section 4.2 provide secure signed routers for networks. Nemo's three prime RSA is faster because of the CRT(section 3.1). Although, Nemo's three prime RSA applies CRT to decryption section, still greater speed could be achieved by applying to both encryption/decryption. Such details are supplied by Quisquater.

42. The RSA paper teaches both *randomness* and *distinctness* are important in the selection of primes for the two prime factors  $p$  and  $q$  scheme that they propose (see Rivest et. al. page 6, line 34 ;page 9, lines 2-3, and line 26-27) in order to maximize security. If the size of the modulus  $n$  is restricted to 200 digits, then maximum security is attained by taking by choose  $p$  and  $q$  differing by a few digits (distinctness) and chosen at random. Thus if randomness and distinctness is not applied to multifactor

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scheme, one loses the randomness that is there are a lot fewer ways to choose a two hundred digit number of the form  $p^2 q$  as opposed to  $pqr$  and hence a loss of security. Thus one of ordinary skill in the art would recognize in order to maximize security one must increase the number of possible choices which implies distinctness of all factors that is  $e_1 = e_2 = e_3 = \dots = e_k$ . Thus one of ordinary skill of the art would have been motivated to combine the general teachings of Lidl with the additional speed enhancements of Quisquater and finally the security teachings of the original RSA paper to obtain a security system which is fast and could run on devices with limited computational resources such as CD ROM's, smartcards, secure net browsers, etc.

Claim 1 is rejected.

43. Claim 18-66 and 73-92 rejected under 35 U.S.C. 103(a) as being unpatentable over Nemo, RSA Moduli Should Have 3 Primes Factors, August 1996, and further in view of Quisquater and Couvreur, Fast Decipherment Algorithm for RSA Public-Key Cryptosystem, 1982) and Rivest et. al. A Method for Obtaining Digital Signatures and Public-key Cryptosystem, Communications of the ACM, 21(2) February 1978, as applied to claim 17 above, and further in view of Ding et. al. The Chinese Remainder Theorem, World Scientific.

44. As per claim 18-21, the details of a recursive (iterative) algorithm is given page

23. Note the relabelling of the dummy indices and the use of the extended Euclidian algorithm  $u_i M_i + v_i m_i = 1$  to provide the inverse  $u_i$  or  $w_i^{-1}$  modulo  $m_k$  or  $p_i$  in 2.8 of the product  $M_k$  corresponding to applicant's  $w_i$ . Claims 18-21 are rejected.

45. Claims 22-26 are a system implementation of claims 17-21 and are rejected in view of the same prior art of record.

46. In claim 17, the limitation of the decomposition into subtasks performed simultaneously, of the RSA decryption equation was applied without any corresponding application of the same technique to the encryption part of the encryption system. The limitations of claims 27 are directed to the same decomposition into subtasks to be performed simultaneously. One of ordinary skill in the art recognizing the same benefits may be had by applying the same mathematics to the encryption area would have been motivated to apply it to the encryption part of the cryptosystem to gain the same benefits. Claim 27 is rejected.

47. As per claims 28-31, expand upon the CRT algorithm applied to this aspect of the encryption and would be rejected on the same group as claims 18-21. Claims 28-31 are rejected.

48. Claims 32-36 are a system implementation of claims 27-31 and are rejected in view of the same prior art of record. Claims 27-31 are rejected.

49. Claims 37-41 and 44 recite a method for decoding corresponding to the method of encoding claims of 17-22 and are rejected in view of the same prior art (all references disclosed both an encoding and decoding scheme). Claim 37-41 and 44 are rejected.

50. As per claims 42-43, and 45-46, the limitation of a cryptographic system for decoding implementing method of claims 37-41, and 44 is rejected in view of the same prior art of record. Claims 42-41 and 44 are rejected.

51. As per claim 47-51, the limitation for a method of generating digital signature is disclosed by Rivest (see pages 4-6) for two prime factors. Using the Lidl/Quisquater/Ding



scheme, one of ordinary skill in the art would have also been motivated to apply the same techniques to digital signature to increase speed, conserve computational resources which are important credit card transactions, and digital rights management. Claims 47-51 are rejected.

52. Claims 52-56 are a system implementation for the generating method recited in claims 47-52 and is rejected in view of the same prior art of record. Claims 52-56

53. As per claims 57-61, the limitations of a process for verifying digital signatures, recited in the method claims 47-52 is disclosed by Rivest (page 5). Claims 57-61 are rejected.

54. Claims 62-66, recite a system for generating and validating digital signatures corresponding to method claims 47-51 and 57-61 and are rejected in view of the same prior art of record.

55. Claims 73, 75, 77, 79, 81, 83, 85, 87, 89, 91 recites the limitation of a plurality of exponentiator units operating substantially simultaneously and performing subtasks are disclosed by Figure 1 Quisquater. Claims 73, 75, 77, 79, 81, 83, 85, 87, 89, 91 are rejected.

56. Claims 74, 76, 78, 80, 82, 84, 86, 88, 90, 92 recite the limitation that each distinct random prime factor has the same number of bits is disclosed in Quisquater page 906 second column under figure 1.

### ***Response to Arguments***

57. Applicant's arguments with respect to claim 17-66 and 73-92 have been considered but are moot in view of the new ground(s) of rejection.

### ***Conclusion***


Any inquiry concerning this communication or earlier communications from the examiner should be directed to James Seal whose telephone number is 703 308 4562. The examiner can normally be reached on M-F, 8-5.

If attempts to reach the examiner by telephone are unsuccessful, the examiner's supervisor, Gail Hayes can be reached on 703 305 9711. The fax phone numbers for the organization where this application or proceeding is assigned are 703 746 7239 for regular communications and 703 746 7240 for After Final communications.

Any inquiry of a general nature or relating to the status of this application or proceeding should be directed to the receptionist whose telephone number is 703 308 3900.

JWS

Jws  
May 1, 2003

  
GAIL HAYES  
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